

Linear Regression

Worksheet for calculating calibration lines
and error analysis

Paste your x,y data into a new spreadsheet

Use the commands shown in the window

The screenshot shows a Microsoft Excel spreadsheet with the following data in columns A and B:

Row	Column A	Column B
1	1	12.07462
2	2	9.233974
3	3	12.15843
4	4	16.57853
5	5	20.97274
6	6	29.09715
7	7	33.25863
8	8	41.74399
9	9	41.13912
10	10	50.75817
11	11	56.78892
12	12	56.35181
13	13	64.1386
14	14	65.80677
15	15	67.08946
16	16	72.97623
17	17	75.96516
18	18	88.01478
19	19	88.61095
20	20	94.56795
21	21	93.12808
22	22	105.4452
23	23	109.5585
24	24	114.3888
25	25	116.3916
26	26	124.648
27	27	126.9922

The UltraEdit-32 window displays the following commands:

```
SELECT H3:I6
=LINEST (B1:B50,A1:A50,1,1)
SELECT H1
=AVERAGE (A1:A50)
SELECT I1
=SUMSQ (A1:A50)
SELECT H8
=TINV (0.05, $I$6)
=A1*$H$3+$I$3
=$H$3*A1+$I$3+$H$8*$I$5*SQRT (1/ ($I$6+2)+ ($I$6+2)* (A1-$H$1)^2/ (( $I$6+2)*$I$1- (( $I$6+2)*$H$1)^2))
=$H$3*A1+$I$3-$H$8*$I$5*SQRT (1/ ($I$6+2)+ ($I$6+2)* (A1-$H$1)^2/ (( $I$6+2)*$I$1- (( $I$6+2)*$H$1)^2))
=$H$3*A1+$I$3+$H$8*$I$5*SQRT (1+1/ ($I$6+2)+ ($I$6+2)* (A1-$H$1)^2/ (( $I$6+2)*$I$1- (( $I$6+2)*$H$1)^2))
=$H$3*A1+$I$3-$H$8*$I$5*SQRT (1+1/ ($I$6+2)+ ($I$6+2)* (A1-$H$1)^2/ (( $I$6+2)*$I$1- (( $I$6+2)*$H$1)^2))
```

SELECT H3:I6

=LINEST(B1:B50,A1:A50,1,1)

SELECT H1

=AVERAGE(A1:A50)

SELECT I1

=SUMSQ(A1:A50)

Make each selection first and then paste the command in black into the spreadsheet header

SELECT H8

=TINV(0.05,\$I\$6)

SELECT C1

=A1*\$H\$3+\$I\$3

THEN CLICK THE LOWER RIGHT CORNER TO FILL THE C COLUMN

**These steps are what you did in the computational Lab to perform the linear regression, calculate the t-test and generate the calculated line
The “trumpets” are on the next page**

SELECT D1

=H\$3*A1+I\$3+H\$8*I\$5*

SQRT(1/(I\$6+2)+(I\$6+2)*(A1-H\$1)^2/((I\$6+2)*I\$1-((I\$6+2)*H\$1)^2))

THEN CLICK THE LOWER RIGHT CORNER TO FILL THE D COLUMN

SELECT E1

=H\$3*A1+I\$3-H\$8*I\$5*

SQRT(1/(I\$6+2)+(I\$6+2)*(A1-H\$1)^2/((I\$6+2)*I\$1-((I\$6+2)*H\$1)^2))

THEN CLICK THE LOWER RIGHT CORNER TO FILL THE E COLUMN

SELECT F1

=H\$3*A1+I\$3+H\$8*I\$5*

SQRT(1+1/(I\$6+2)+(I\$6+2)*(A1-H\$1)^2/((I\$6+2)*I\$1-((I\$6+2)*H\$1)^2))

THEN CLICK THE LOWER RIGHT CORNER TO FILL THE F COLUMN

SELECT G1

=H\$3*A1+I\$3-H\$8*I\$5*S

QRT(1+1/(I\$6+2)+(I\$6+2)*(A1-H\$1)^2/((I\$6+2)*I\$1-((I\$6+2)*H\$1)^2))

THEN CLICK THE LOWER RIGHT CORNER TO FILL THE G COLUMN

Follow the cell designation H3:I6 exactly

Also specify the number of data points

The screenshot shows the Microsoft Excel interface with the following data and formula:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	
1	1	12.07462																			
2	2	9.233974																			
3	3	12.15843																			
4	4	16.57853																			
5	5	20.97274																			
6	6	29.09715																			
7	7	33.25863																			
8	8	41.74399																			
9	9	41.13912																			
10	10	50.75817																			
11	11	56.78892																			
12	12	56.35181																			
13	13	64.1386																			
14	14	65.80677																			
15	15	67.08946																			
16	16	72.97623																			
17	17	75.96516																			
18	18	88.01478																			
19	19	88.61095																			
20	20	94.56795																			
21	21	93.12808																			
22	22	105.4452																			
23	23	109.5585																			
24	24	114.3888																			
25	25	116.3916																			
26	26	124.648																			
27	27	126.9922																			

Formula bar: `=LINEST(B1:B50,A1:A50,1,1)`

Cell H3:I6 contains: `50,1,1)`

Change A50 and B50 to meet your needs

Ctrl-Shift-Enter

The screenshot shows an Excel spreadsheet with a data table in columns A and B, and a LINEST array formula result in columns H and I. The formula bar shows `{=LINEST(B1:B50,A1:A50,1,1)}`. The data table consists of 27 rows of values. The LINEST result is a 4x2 array of values.

Row	Column A	Column B	Column H	Column I
1	1	12.07462		
2	2	9.233974		
3	3	12.15843	4.501697	2.767986
4	4	16.57853	0.030069	0.881015
5	5	20.97274	0.997863	3.068249
6	6	29.09715	22414.36	48
7	7	33.25863		
8	8	41.74399		
9	9	41.13912		
10	10	50.75817		
11	11	56.78892		
12	12	56.35181		
13	13	64.1386		
14	14	65.80677		
15	15	67.08946		
16	16	72.97623		
17	17	75.96516		
18	18	88.01478		
19	19	88.61095		
20	20	94.56795		
21	21	93.12808		
22	22	105.4452		
23	23	109.5585		
24	24	114.3888		
25	25	116.3916		
26	26	124.648		
27	27	126.9922		

Put the average of the A column in H1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do... Sign in

SUM X ✓ fx =AVERAGE(A1:A50)

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T
1	1	12.07462						A1:A50												
2	2	9.233974																		
3	3	12.15843						4.501697	2.767986											
4	4	16.57853						0.030069	0.881015											
5	5	20.97274						0.997863	3.068249											
6	6	29.09715						22414.36	48											
7	7	33.25863																		
8	8	41.74399																		
9	9	41.13912																		
10	10	50.75817																		
11	11	56.78892																		
12	12	56.35181																		
13	13	64.1386																		
14	14	65.80677																		
15	15	67.08946																		
16	16	72.97623																		
17	17	75.96516																		
18	18	88.01478																		
19	19	88.61095																		
20	20	94.56795																		
21	21	93.12808																		
22	22	105.4452																		
23	23	109.5585																		
24	24	114.3888																		
25	25	116.3916																		
26	26	124.648																		
27	27	126.9922																		

Change A50 to meet your needs

Sheet1

Edit

5:08 PM 1/19/2019

Put the sum of squares of the A column in I1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

SUM X ✓ fx =SUMSQ(A1:A50)

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
1	1	12.07462						25.5	A1:A50										
2	2	9.233974																	
3	3	12.15843						4.501697	2.767986										
4	4	16.57853						0.030069	0.881015										
5	5	20.97274						0.997863	3.068249										
6	6	29.09715						22414.36	48										
7	7	33.25863																	
8	8	41.74399																	
9	9	41.13912																	
10	10	50.75817																	
11	11	56.78892																	
12	12	56.35181																	
13	13	64.1386																	
14	14	65.80677																	
15	15	67.08946																	
16	16	72.97623																	
17	17	75.96516																	
18	18	88.01478																	
19	19	88.61095																	
20	20	94.56795																	
21	21	93.12808																	
22	22	105.4452																	
23	23	109.5585																	
24	24	114.3888																	
25	25	116.3916																	
26	26	124.648																	
27	27	126.9922																	

Change A50 to meet your needs

Sheet1

Place the calculated regression line in C1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

SUM X ✓ fx =A1*\$H\$3+\$I\$3

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S
1	1	12.07462	\$3+\$I\$3					25.5	42925										
2	2	9.233974																	
3	3	12.15843						4.501697	2.767986										
4	4	16.57853						0.030069	0.881015										
5	5	20.97274						0.997863	3.068249										
6	6	29.09715						22414.36	48										
7	7	33.25863																	
8	8	41.74399						2.010635											
9	9	41.13912																	
10	10	50.75817																	
11	11	56.78892																	
12	12	56.35181																	
13	13	64.1386																	
14	14	65.80677																	
15	15	67.08946																	
16	16	72.97623																	
17	17	75.96516																	
18	18	88.01478																	
19	19	88.61095																	
20	20	94.56795																	
21	21	93.12808																	
22	22	105.4452																	
23	23	109.5585																	
24	24	114.3888																	
25	25	116.3916																	
26	26	124.648																	
27	27	126.9922																	

Sheet1

Edit



Place calculated upper confidence curve in D1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

D1 $=\$H\$3*A1+\$I\$3+\$H\$8*\$I\$5*\text{SQRT}(1/(\$I\$6+2)+(\$I\$6+2)*(A1-\$H\$1)^2/((\$I\$6+2)*\$I\$1-((\$I\$6+2)*\$H\$1)^2))$

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
1	1	12.07462	7.269683	8.988724				25.5	42925									
2	2	9.233974																
3	3	12.15843						4.501697	2.767986									
4	4	16.57853						0.030069	0.881015									
5	5	20.97274						0.997863	3.068249									
6	6	29.09715						22414.36	48									
7	7	33.25863																
8	8	41.74399						2.010635										
9	9	41.13912																
10	10	50.75817																
11	11	56.78892																
12	12	56.35181																
13	13	64.1386																
14	14	65.80677																
15	15	67.08946																
16	16	72.97623																
17	17	75.96516																
18	18	88.01478																
19	19	88.61095																
20	20	94.56795																
21	21	93.12808																
22	22	105.4452																
23	23	109.5585																
24	24	114.3888																
25	25	116.3916																
26	26	124.648																
27	27	126.9922																

Sheet1

Place calculated lower confidence curve in E1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

SUM X ✓ fx $=\$H\$3*A1+\$I\$3-\$H\$8*\$I\$5*\text{SQRT}(1/(\$I\$6+2)+(\$I\$6+2)*(A1-\$H\$1)^2/((\$I\$6+2)*\$I\$1-((\$I\$6+2)*\$H\$1)^2))$

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
1	1	12.07462	7.269683	8.988724	=\$I1^2))			25.5	42925									
2	2	9.233974																
3	3	12.15843						4.501697	2.767986									
4	4	16.57853						0.030069	0.881015									
5	5	20.97274						0.997863	3.068249									
6	6	29.09715						22414.36	48									
7	7	33.25863																
8	8	41.74399						2.010635										
9	9	41.13912																
10	10	50.75817																
11	11	56.78892																
12	12	56.35181																
13	13	64.1386																
14	14	65.80677																
15	15	67.08946																
16	16	72.97623																
17	17	75.96516																
18	18	88.01478																
19	19	88.61095																
20	20	94.56795																
21	21	93.12808																
22	22	105.4452																
23	23	109.5585																
24	24	114.3888																
25	25	116.3916																
26	26	124.648																
27	27	126.9922																

Sheet1

Place calculated upper prediction curve in F1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

F1 : $=\$H\$3*A1+\$I\$3+\$H\$8*\$I\$5*\text{SQRT}(1+1/(\$I\$6+2)+(\$I\$6+2)*(A1-\$H\$1)^2/((\$I\$6+2)*\$I\$1-((\$I\$6+2)*\$H\$1)^2))$

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
1	1	12.07462	7.269683	8.988724	5.550642	13.67384		25.5	42925									
2	2	9.233974																
3	3	12.15843						4.501697	2.767986									
4	4	16.57853						0.030069	0.881015									
5	5	20.97274						0.997863	3.068249									
6	6	29.09715						22414.36	48									
7	7	33.25863																
8	8	41.74399						2.010635										
9	9	41.13912																
10	10	50.75817																
11	11	56.78892																
12	12	56.35181																
13	13	64.1386																
14	14	65.80677																
15	15	67.08946																
16	16	72.97623																
17	17	75.96516																
18	18	88.01478																
19	19	88.61095																
20	20	94.56795																
21	21	93.12808																
22	22	105.4452																
23	23	109.5585																
24	24	114.3888																
25	25	116.3916																
26	26	124.648																
27	27	126.9922																

Sheet1

Ready

Place calculated lower prediction curve in G1

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

SUM X ✓ fx $=\$H\$3*A1+\$I\$3-\$H\$8*\$I\$5*\text{SQRT}(1+1/(\$I\$6+2)+(\$I\$6+2)*(A1-\$H\$1)^2/((\$I\$6+2)*\$I\$1-((\$I\$6+2)*\$H\$1)^2))$

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
1	1	12.07462	7.269683	8.988724	5.550642	13.67384	(\$I^2))	25.5	42925								
2	2	9.233974															
3	3	12.15843						4.501697	2.767986								
4	4	16.57853						0.030069	0.881015								
5	5	20.97274						0.997863	3.068249								
6	6	29.09715						22414.36	48								
7	7	33.25863															
8	8	41.74399						2.010635									
9	9	41.13912															
10	10	50.75817															
11	11	56.78892															
12	12	56.35181															
13	13	64.1386															
14	14	65.80677															
15	15	67.08946															
16	16	72.97623															
17	17	75.96516															
18	18	88.01478															
19	19	88.61095															
20	20	94.56795															
21	21	93.12808															
22	22	105.4452															
23	23	109.5585															
24	24	114.3888															
25	25	116.3916															
26	26	124.648															
27	27	126.9922															

Sheet1

Select C1-G1 and double click lower right corner

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

C1 : X ✓ fx =A1*\$H\$3+\$I\$3

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
1	1	12.07462	7.269683	8.988724	5.550642	13.67384	0.865526	25.5	42925								
2	2	9.233974															
3	3	12.15843						4.501697	2.767986								
4	4	16.57853						0.030069	0.881015								
5	5	20.97274						0.997863	3.068249								
6	6	29.09715						22414.36	48								
7	7	33.25863															
8	8	41.74399						2.010635									
9	9	41.13912															
10	10	50.75817															
11	11	56.78892															
12	12	56.35181															
13	13	64.1386															
14	14	65.80677															
15	15	67.08946															
16	16	72.97623															
17	17	75.96516															
18	18	88.01478															
19	19	88.61095															
20	20	94.56795															
21	21	93.12808															
22	22	105.4452															
23	23	109.5585															
24	24	114.3888															
25	25	116.3916															
26	26	124.648															
27	27	126.9922															
28	28	131.6666															

Sheet1

Ready Average: 7.269683123 Count: 5 Sum: 36.34841561

This fills all values down to the bottom of data

Book2 - Excel (Product Activation Failed)

File Home Insert Page Layout Formulas Data Review View Tell me what you want to do...

C1 \times \checkmark $\&x$ $=A1*\$H\$3+\$I\3

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q
1	1	12.07462	7.269683	8.988724	5.550642	13.67384	0.865526	25.5	42925								
2	2	9.233974	11.77138	13.43861	10.10415	18.16183	5.380935										
3	3	12.15843	16.27308	17.8891	14.65705	22.65035	9.8958	4.501697	2.767986								
4	4	16.57853	20.77477	22.34025	19.2093	27.13943	14.41012	0.030069	0.881015								
5	5	20.97274	25.27647	26.79212	23.76082	31.62905	18.92389	0.997863	3.068249								
6	6	29.09715	29.77817	31.24479	28.31154	36.11923	23.4371	22414.36	48								
7	7	33.25863	34.27986	35.69835	32.86138	40.60997	27.94976										
8	8	41.74399	38.78156	40.15288	37.41024	45.10126	32.46186	2.010635									
9	9	41.13912	43.28326	44.60849	41.95802	49.59312	36.97339										
10	10	50.75817	47.78496	49.0653	46.50461	54.08554	41.48437										
11	11	56.78892	52.28665	53.52344	51.04987	58.57853	45.99477										
12	12	56.35181	56.78835	57.98304	55.59365	63.07209	50.50461										
13	13	64.1386	61.29005	62.44428	60.13581	67.56622	55.01387										
14	14	65.80677	65.79174	66.90733	64.67615	72.06093	59.52256										
15	15	67.08946	70.29344	71.37239	69.21449	76.55621	64.03067										
16	16	72.97623	74.79514	75.83966	73.75061	81.05207	68.53821										
17	17	75.96516	79.29683	80.30937	78.28429	85.5485	73.04516										
18	18	88.01478	83.79853	84.78177	82.81529	90.04552	77.55154										
19	19	88.61095	88.30023	89.25709	87.34336	94.54312	82.05733										
20	20	94.56795	92.80192	93.73559	91.86826	99.0413	86.56254										
21	21	93.12808	97.30362	98.2175	96.38974	103.5401	91.06717										
22	22	105.4452	101.8053	102.7031	100.9076	108.0394	95.57121										
23	23	109.5585	106.307	107.1925	105.4216	112.5394	100.0747										
24	24	114.3888	110.8087	111.6859	109.9316	117.0399	104.5775										
25	25	116.3916	115.3104	116.1834	114.4374	121.541	109.0798										
26	26	124.648	119.8121	120.6851	118.9391	126.0427	113.5815										
27	27	126.9922	124.3138	125.1909	123.4367	130.545	118.0826										

Sheet1

Ready Average: 117.5612567 Count: 250 Sum: 29390.31418

Done

