The structure of porphine is shown in the figure. To understand the absorption spectra of hemoglobin, one can use a free electron model for a particle on a circle. In the free electron model you may assume that the electrons from the p-orbitals of the carbon atoms populate energy levels derived from the particle-on-a-circle solution to the Schrödinger equation.



A. Assuming that the radius of the circle is 3.5 Å and that the porphyrin has 18 electrons, please draw an energy level diagram for this system.



B. Calculate the maximum of the absorption spectrum (in nm).

Solution: Using the particle-on-a-circle model

$$\Delta E = \frac{h}{8\pi^2 c m_e R^2} (m_e^2 - m_g^2)$$

 $\Delta E = 6.626 \times 10^{-34} \text{Js}/[8(3.14159)^2(9.1 \times 10^{-31} \text{ kg})(2.99 \times 10^{10} \text{ cm/s})(3.5 \times 10^{-10} \text{ m})^2](5^2-4^2)$ 

= 22,660 cm<sup>-1</sup> (which corresponds to 441 nm)

 $\lambda_{max} = \underline{\qquad} nm.$