The maturation of immunoglobulins involves a folding pathway followed by dimerization. The mechanism is:

$$k_{1} \quad k_{2}$$

$$U \leftrightarrow I \rightarrow N$$

$$k_{-1}$$

$$k_{3}$$

$$2N \rightarrow F_{2}$$

a.) Write down the rate equations for each of the species in this rate scheme.

b.) Assuming that $k_2 \gg k_1$ and $k_3 \gg k_2$ determine an expression for the rate of formation of the folded immunoglobulin dimer F_2 as a function of the concentration of the starting unfolded monomer [U].

a.) Write down the rate equations for each of the species in this rate scheme.

Solution:

d

$$\frac{d[U]}{dt} = -k_1[U] + k_{-1}[I]$$

$$\frac{[I]}{dt} = -(k_{-1} + k_2)[I] + k_1[U]$$

$$\frac{d[N]}{dt} = k_2[I] - k_3[N]^2$$

$$\frac{d[F_2]}{dt} = k_3[N]^2$$

b.) Assuming that $k_2 \gg k_1$ and $k_3 \gg k_2$ determine an expression for the rate of formation of the folded immunoglobulin dimer F_2 as a function of the concentration of the starting unfolded monomer [U].

Solution: Apply the steady state approximation to the dimeric intermediate I and N.

$$\frac{d[I]}{dt} = -(k_{-1} + k_2)[I] + k_1[U] \approx 0$$

$$\frac{\mathrm{d}[\mathrm{N}]}{\mathrm{d}\mathrm{t}} = \mathrm{k}_2[\mathrm{I}] - \mathrm{k}_3[\mathrm{N}]^2 \approx 0$$

$$[I] = \frac{k_1[U]}{k_{-1} + k_2}$$

b.) Assuming that $k_2 >> k_1$ and $k_3 >> k_2$ determine an expression for the rate of formation of the folded immunoglobulin dimer F_2 as a function of the concentration of the starting unfolded monomer [U]. Complete the substutions to solve for an expression for the

final folded immunoglobulin dimer.

$$k_{3}[N]^{2} = k_{2}[I] = \frac{k_{1}k_{2}[U]}{(k_{-1} + k_{2})}$$
$$\frac{d[F_{2}]}{dt} = \frac{k_{1}k_{2}[U]}{(k_{-1} + k_{2})}$$