Barnase is a two-state protein that is denatured in guanidium hydrochloride (GdnHCl). Barnase is 50% unfolded in 3 M GdnHCl, but 99% folded in 0.03 M GdnHCl. If 3 M solution of Barnase is diluted by a factor of 100 (i.e. to 0.03 M) it is observed to reach its new equilibrium in 12 minutes. What is the folding rate constant of this protein?

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Solution: Use microscopic reversibility

$$K = \frac{k_f}{k_u}$$

And the observed rate constant for approach to equilibrium

$$k_{obs} = k_f + k_u = k_f + \frac{k_f}{K} = k_f \left(1 + \frac{1}{K}\right)$$

Insert the given values to calculate the folding rate constant

$$k_f = \frac{k_{obs}}{\left(1 + \frac{1}{K}\right)} = \frac{1}{\tau_{obs}\left(1 + \frac{fu}{ff}\right)}$$

where fu = fraction unfolded and ff = fraction folded.

$$k_f = \frac{1}{(12 \text{ min.}) \left(1 + \frac{1}{99}\right)} = 0.0825 \text{ min}^{-1}$$

To put this another way, the folding time (which is the inverse of the folding rate constant) is approximately 12.1 minutes.

Note on the estimation of the equilibrium constant. The process being considered is a folding equilibrium:

$$u \rightarrow f$$

The equilibrium constant is:

$$K = \frac{[f]}{[u]} = \frac{ff}{fu}$$

We can use the ratio of the fraction in place of the ratio of concentrations.