## Chemistry 201

#### Weak Acids and Bases

### NC State University



### pH of Weak Acids & Bases

- How do we find  $[H_3O^{1+}]$ ?
- How do acid and base strengths relate?

Relationship of pK<sub>a</sub> and pK<sub>b</sub>  

$$HA + H_2 0 \leftrightarrow A^- + H_3 0^+ \qquad K_a = \frac{[A^-][H^+]}{[HA]}$$

$$A^- + H_2 0 \leftrightarrow HA + OH^- \qquad K_b = \frac{[HA][OH^-]}{[A^-]}$$

$$H_2 0 + H_2 0 \leftrightarrow OH^- + H_3 0^+ \qquad K_w = [H^+][OH^-]$$

$$\left(\frac{[A^-][H^+]}{[HA]}\right) \left(\frac{[HA][OH^-]}{[A^-]}\right) = [H^+][OH^-]$$

$$K_a K_b = K_w$$

$$pK_a + pK_b = pK_w$$

### Calculation of the pH of weak acids

For a generic weak acid dissociation in water to produce ions we can consider the general case,

$$HA \leftrightarrow A^- + H^+$$

in which the initial concentration of [HA] = C and  $[A^-] = [H^+] = 0$ . Then we make the following reaction table:

Molecule	HA	$A^{-}$	$H^+$
Initial	С	0	0
Change	-X	Х	х
Equilibrium	C-x	x	Х

# Using the $K_a$ to obtain $x = [H^+]$

We can substitute these values into  $K_a$ ,

$$K_a = \frac{x^2}{C - x}$$

This can be formulated as a general quadratic equation.

$$K_a C - K_a x - x^2 = 0$$

Note that we do not necessarily need to use the quadratic Formula. If C >> x then we can use an approximation

$$x \approx \sqrt{CK_a}$$

Which is justified on the next slide.

### Justification of approximate solution

The general case has a solution

$$x = \frac{K_a \pm \sqrt{K_a^2 + 4CK_a}}{-2}$$

If the concentration C of the acid is sufficiently large, then we can neglect x relative to x, i.e. C >> x. In this case,

$$K_a \approx \frac{x^2}{C}$$

and

$$x \approx \sqrt{CK_a}$$

# What is the pH of a 0.20 M solution of $HC_2H_3O_2$ ? (pK<sub>a</sub> = 4.74)

# What is the pH of a 0.20 M solution of $HC_2H_3O_2$ ? (pK<sub>a</sub> = 4.74)

Solution: Set  $A = HC_2H_3O_2$ 

 $HA \rightarrow H^+ + A^-$ 

Step 1: Solve for  $K_a = 1.82 \times 10^{-5}$ Step 2: Make a reaction table

Molecule	HA	A⁻	H <sup>+</sup>
Initial	0.2	0	0
Difference	-X	X	X
Equilibrium	0.2-x	X	X

# What is the pH of a 0.20 M solution of $HC_2H_3O_2$ ? (pK<sub>a</sub> = 4.74)

Step 3: Solve for x

$$K_{a} = \frac{[A^{-}][H^{+}]}{[HA]} = \frac{x^{2}}{0.2 - x}$$

$$K_{a}(0.2 - x) - x^{2} = 0 \qquad K_{a}0.2 - K_{a}x - x^{2} = 0$$

$$x = \frac{K_{a} \pm \sqrt{K_{a}^{2} + 4(0.2)K_{a}}}{-2}$$

$$x = \frac{1.82x10^{-5} \pm \sqrt{(1.82x10^{-5})^{2} + 0.8(1.82x10^{-5})}}{-2}$$

$$x = 0.00189$$

# What is the pH of a 0.20 M solution of $HC_2H_3O_2$ ? (pK<sub>a</sub> = 4.74)

Step 3. Calculate pH

 $pH = -log_{10}(0.00189) = 2.72$ 

We could have used the approximate method for this acid since x = 0.00189 and C = 0.2. According to the approximate method.

 $x \approx \sqrt{CK_a} = \sqrt{(0.2)(1.82 \ x \ 10^{-5})} = 0.00190$ 

The difference from the exact method is less than 1%.



# pH of Weak Bases What is the pH of a 0.10 M solution of NaF? ( $pK_a = 3.14$ for HF)

Solution: Write down the conjugate base reaction  $F^- + H_2 0 \leftrightarrow HF + 0H^-$ 

Step 1: Solve for K<sub>b</sub>

 $K_b = 10^{-pKb} = 10^{-10.86} = 1.38x10^{-11}$ 

pKb = pKw - pKapKb = 14 - 3.14 = 10.86

## pH of Weak Bases

### NaF problem(contd) ( $pK_a = 3.14$ for HF)

Step 2: Make a reaction table

Molecule	F⁻	HF	OH-
Initial	0.1	0	0
Difference	-X	X	X
Equilibrium	0.1-x	X	X

Step 3: Solve for x  $K_b 0.1 - K_b x - x^2 = 0$   $x = \frac{K_b \pm \sqrt{K_b^2 + 4(0.1)K_b}}{-2}$   $x = 1.17x10^{-6}$  $x = \frac{1.38x10^{-11} \pm \sqrt{(1.38x10^{-11})^2 + 0.4(1.38x10^{-11})}}{-2}$  pH of Weak Bases NaF problem(contd) (pK<sub>a</sub> = 3.14 for HF) Step 4: Solve for pOH

 $pOH = -log_{10}(1.17x10^{-6}) = 5.93$ 

Step 5: Convert to pH

 $pH + pOH = pK_w$ 

 $pH = pK_w - pOH$ 

pH = 14 - 5.93 = 8.07

### pH of Weak Bases

NaF problem(contd) ( $pK_a = 3.14$  for HF) Here again we could have used the approximate method and saved a lot of work.

$$x \approx \sqrt{CK_b} = \sqrt{(0.1)(1.38 \times 10^{-11})} = 1.17 \times 10^{-6}$$

Since Kb is so small in this case the difference is less than one part in 1000.



