## Chemistry 201

## Absolute temperature <br> Temperature conversion Ideal gas law

## NC State University

## Absolute Temperature

We will use the absolute temperature scale (Kelvin) for all chemical calculations. Why? One important reason is that the absolute temperature is proportional to the kinetic energy of a substance.

$$
\mathrm{K}=\frac{3}{2} \mathrm{nRT}
$$

$K$ stands for kinetic energy, $R$ is the gas constant and $n$ is the number of moles.

$$
\frac{1}{2} \mathrm{Nmv}^{2}=\frac{3}{2} \mathrm{nRT}
$$

N is the number of molecules.

## Temperature scales

The absolute scale in Kelvins is offset from the Celsius scale by 273.16 degrees, meaning that $0^{\circ} \mathrm{C} \sim 273 \mathrm{~K}$ to three significant figures. This value is accurate enough for our purposes. Therefore, we can use the formula

$$
K={ }^{o} C+273
$$

The Celsius scale is used by every country in the world as the temperature scale (except the United States). We use the Fahrenheit scale.

## Conversion from Fahrenheit to Celsius

The zero of the Celsius scale occurs at $32^{\circ} \mathrm{F}$ and the The boiling point of water $\left(100^{\circ} \mathrm{C}\right)$ occurs as $212{ }^{\circ} \mathrm{F}$. This means that one degree Celsius is exacly $9 / 5$ times one degree Fahrenheit.

$$
{ }^{\mathrm{o}} \mathrm{C}=\frac{5}{9}\left({ }^{\mathrm{o}} \mathrm{~F}-32\right)
$$

For common values it is useful to have recall that $50^{\circ} \mathrm{F}=10^{\circ} \mathrm{C}, 68^{\circ} \mathrm{F}=20^{\circ} \mathrm{C}$ and $86^{\circ} \mathrm{F}=30^{\circ} \mathrm{C}$. Body temperature is exactly $98.6^{\circ} \mathrm{F}=37.00^{\circ} \mathrm{C}$.

## Ideal gas law

The number of moles, $n$, appears in the ideal gas law:

$$
P V=n R T
$$

This is an equation of state, which means it relates the variables of state, pressure, volume, and temperature.
$R$ is a constant known as the universal gas constant.

$$
\mathrm{R}=8.31 \mathrm{~J} / \mathrm{mol}-\mathrm{K} \text { or } \mathrm{R}=0.08206 \mathrm{~L}-\mathrm{atm} / \mathrm{mol}-\mathrm{K}
$$

Note that the units of the ideal gas law are units of energy.

## The ideal gas law as an energy equation

At first PV may not look like an energy. However, when a fuel is combusted (for example in the cylinder of a car engine), it builds up a pressure, which causes an expansion, an increase in volume. Pressure-volume work is the how engines propel cars. Temperature also represents an energy. The temperature of a gas is proportional to the kinetic energy of the gas molecules. nRT is actually an energy term as can be seen from the units of $R$.

## Solving for the number of moles

We can use the ideal gas law to obtain the number of moles of a gas, provided we are given $\mathrm{P}, \mathrm{V}$ and T . The formula is:

$$
n=\frac{P V}{R T}
$$

For example, how moles are present in 22.4 liters of gas at 273 K and at sea level.
Solution: At sea level, $\mathrm{P}=1 \mathrm{~atm}$ so

$$
n=\frac{P V}{R T}=\frac{(1 \mathrm{~atm})(22.4 \mathrm{~L})}{\left(0.08206 \frac{\mathrm{Latm}}{\mathrm{molK}}\right)(298 \mathrm{~K})}
$$

## Molar gas volume

The solution to the problem is $n=1.0$.
We conclude that one mole has a volume of 22.4 liters
at 273 K . We call this the molar gas volume.
Note that the molar gas volume changes with
temperature.
Problem: Calculate the molar gas volume at 373 K .

